

The 4<sup>th</sup> Joint Meeting of US-Japan Cooperation National Research

Earthquake Research Panel, November 6-8, 2002

- Morioka, Japan -

# **Recipe for Predicting Strong Ground Motion from Inland and Subduction-Zone Earthquakes**

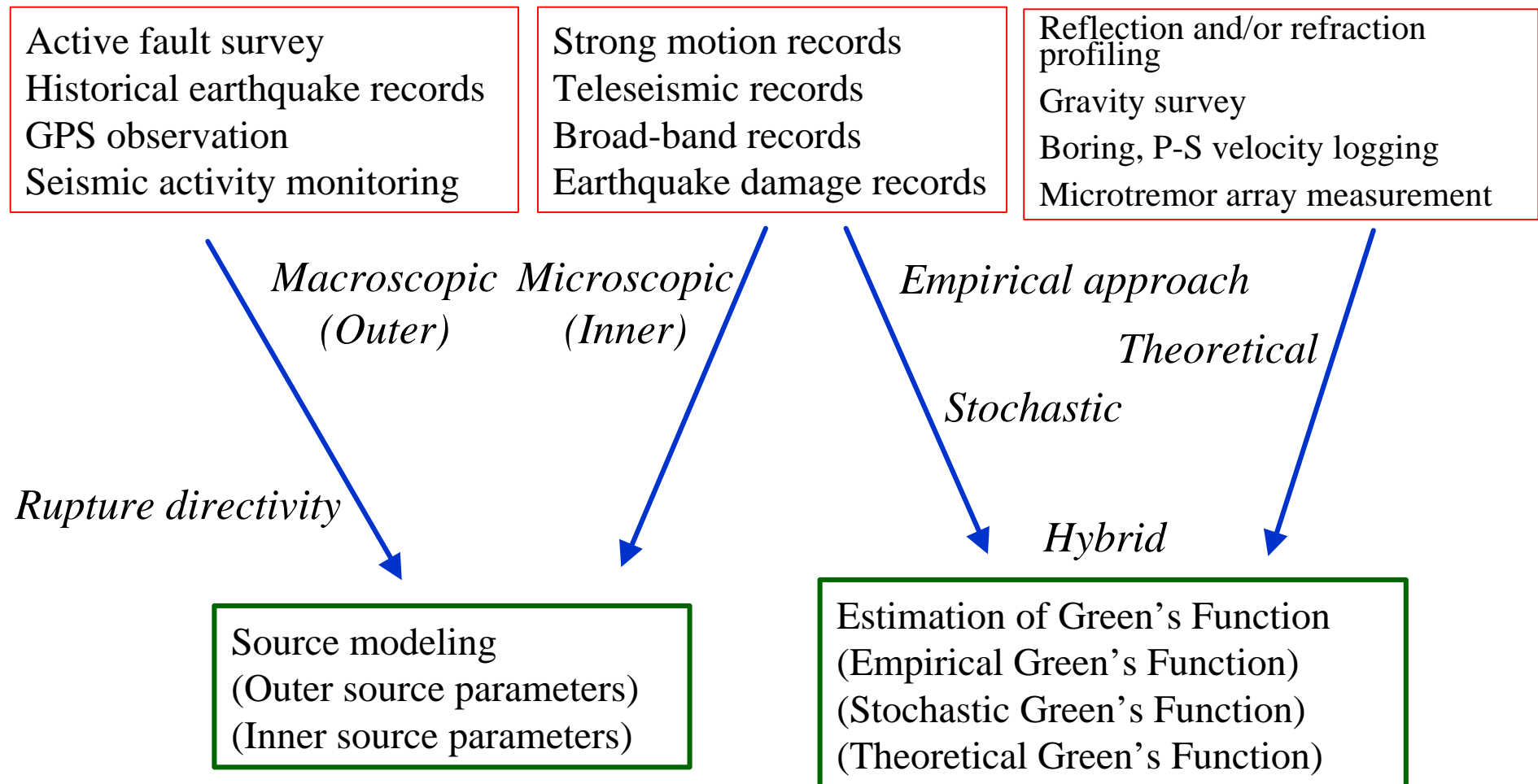
Kojiro Irikura, Hiroe Miyake, Tomotaka Iwata,  
Katsuhiro Kamae, and Hidenori Kawabe

# Framework of predicting strong ground motions for scenario earthquakes

1. Long-term forecasting of earthquakes

2. Strong motion observation and waveform inversion of source process

3. Investigation of underground structures



Source modeling  
(Outer source parameters)  
(Inner source parameters)

Estimation of Green's Function  
(Empirical Green's Function)  
(Stochastic Green's Function)  
(Theoretical Green's Function)

4. Ground motion simulation for  
scenario earthquakes

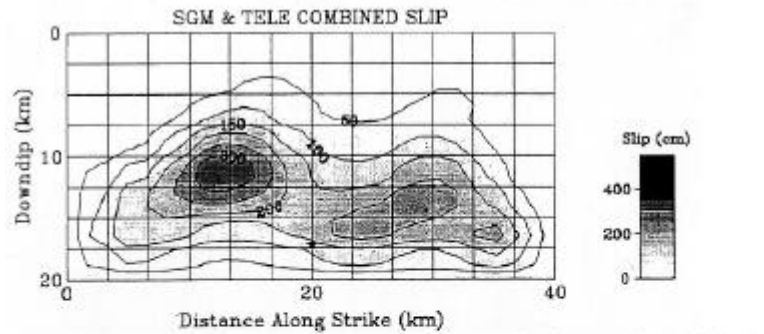
5. Setting seismic  
design criteria

Ground motion waveform  
PGA, PGV  
Response spectra  
Seismic intensity

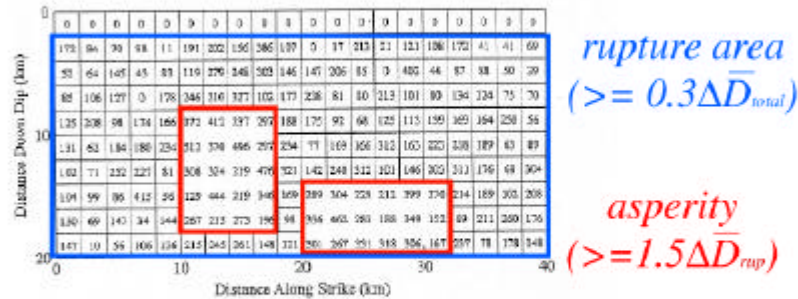
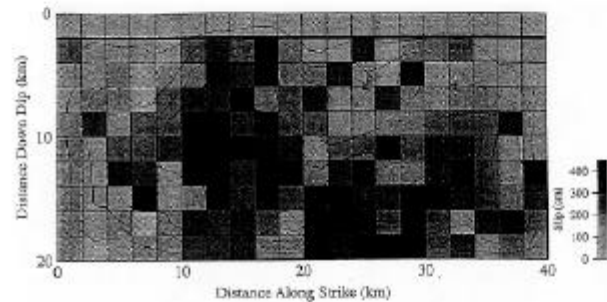
Building codes  
Bridge  
Dam  
Nuclear power plants

**Validation by historical records of earthquake damage**

# Slip Heterogeneity from Waveform Inversion of Strong Motion Records



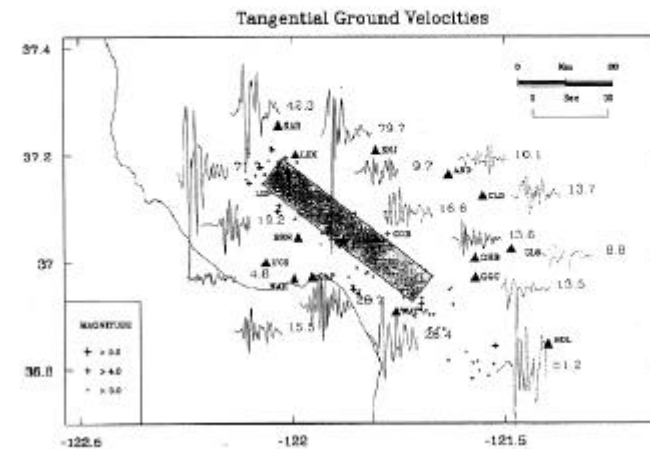
Wald et al. (1991)



Trim Line  
Asperity  
Slip in cm

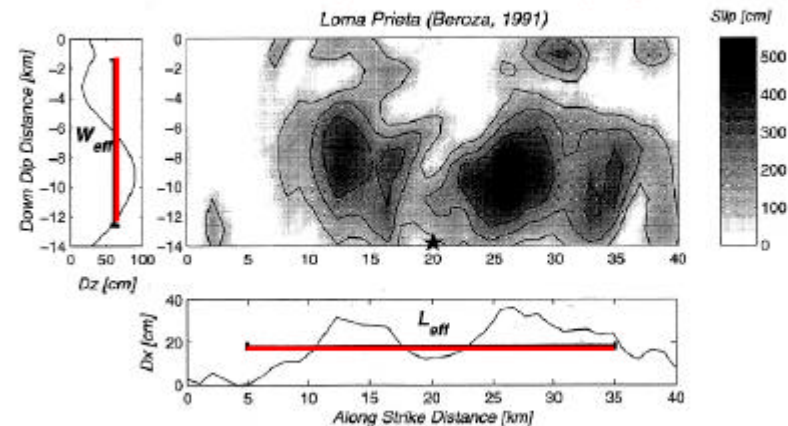
Somerville et al. (1999)

1989 Loma Prieta earthquake ( $M_w 6.9$ )

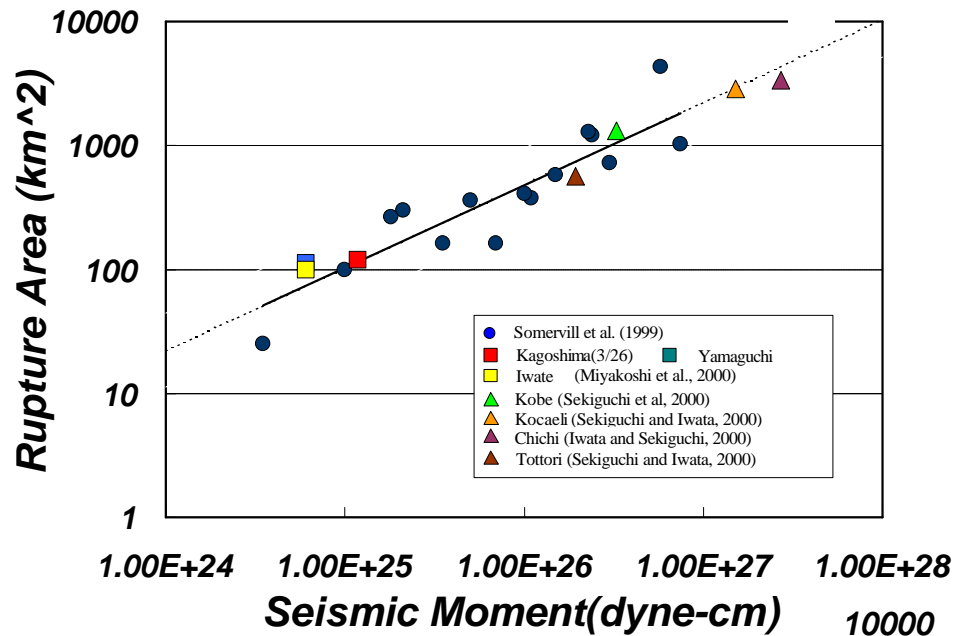


effective source dimension

( $L_{eff}$ ,  $W_{eff}$  are derived by auto-correlation of slip distribution)



Mai and Beroza (2000)

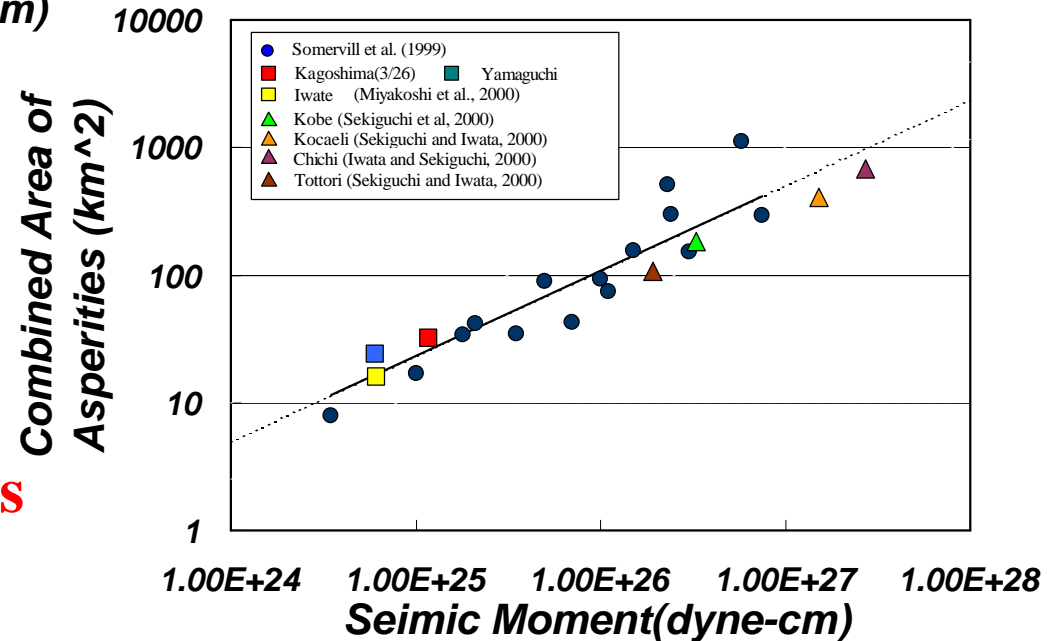


*Relation between  
Rupture Area and  $M_0$*

→ **Outer Fault Parameters**

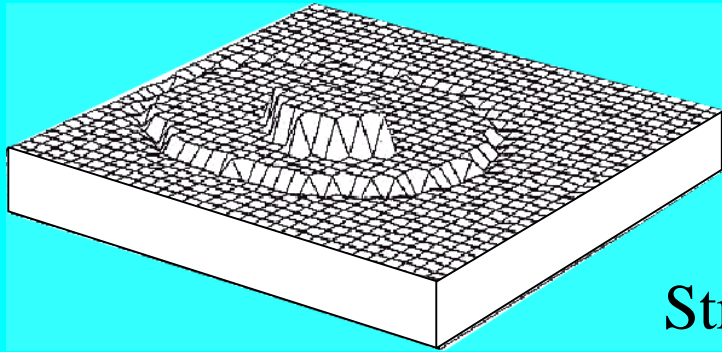
*Relation between  
Combined Area of  
Asperities and  $M_0$*

→ **Inner Fault Parameters**

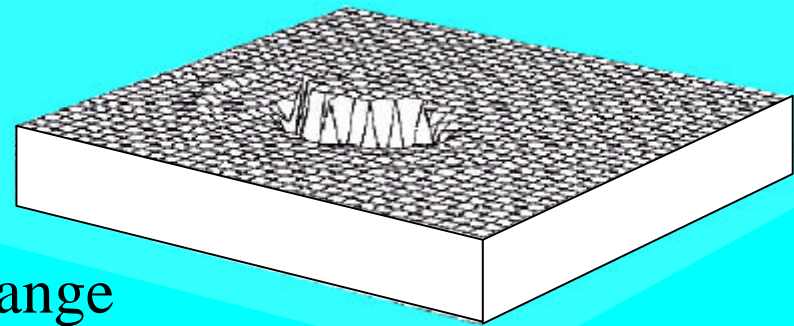


Somerville *et al.* (1999) and Miyakoshi *et al.* (2001)

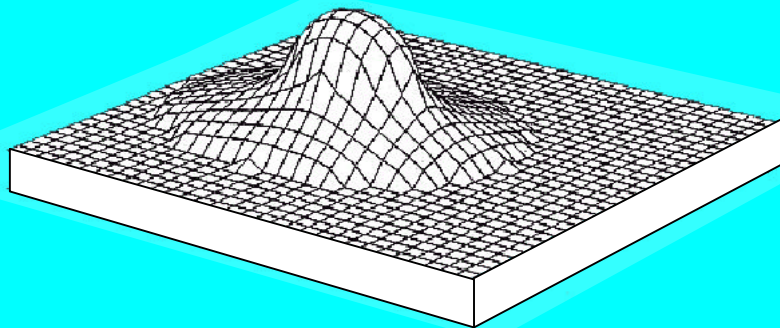
Asperity



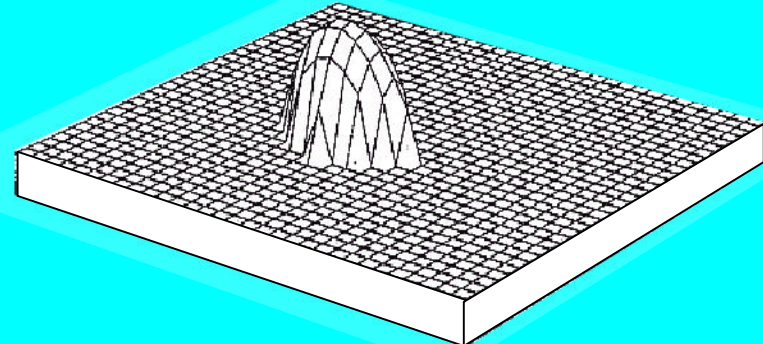
Crack



Stress change



Slip



*Boatwright (1988)*

## Recipe Combined with Dynamic Asperity-Source Model (Irikura et al., 2002)

Strong ground motions are estimated from **inner fault parameters** for fault heterogeneity as well as **outer fault parameters** for entire rupture area and total seismic moment.

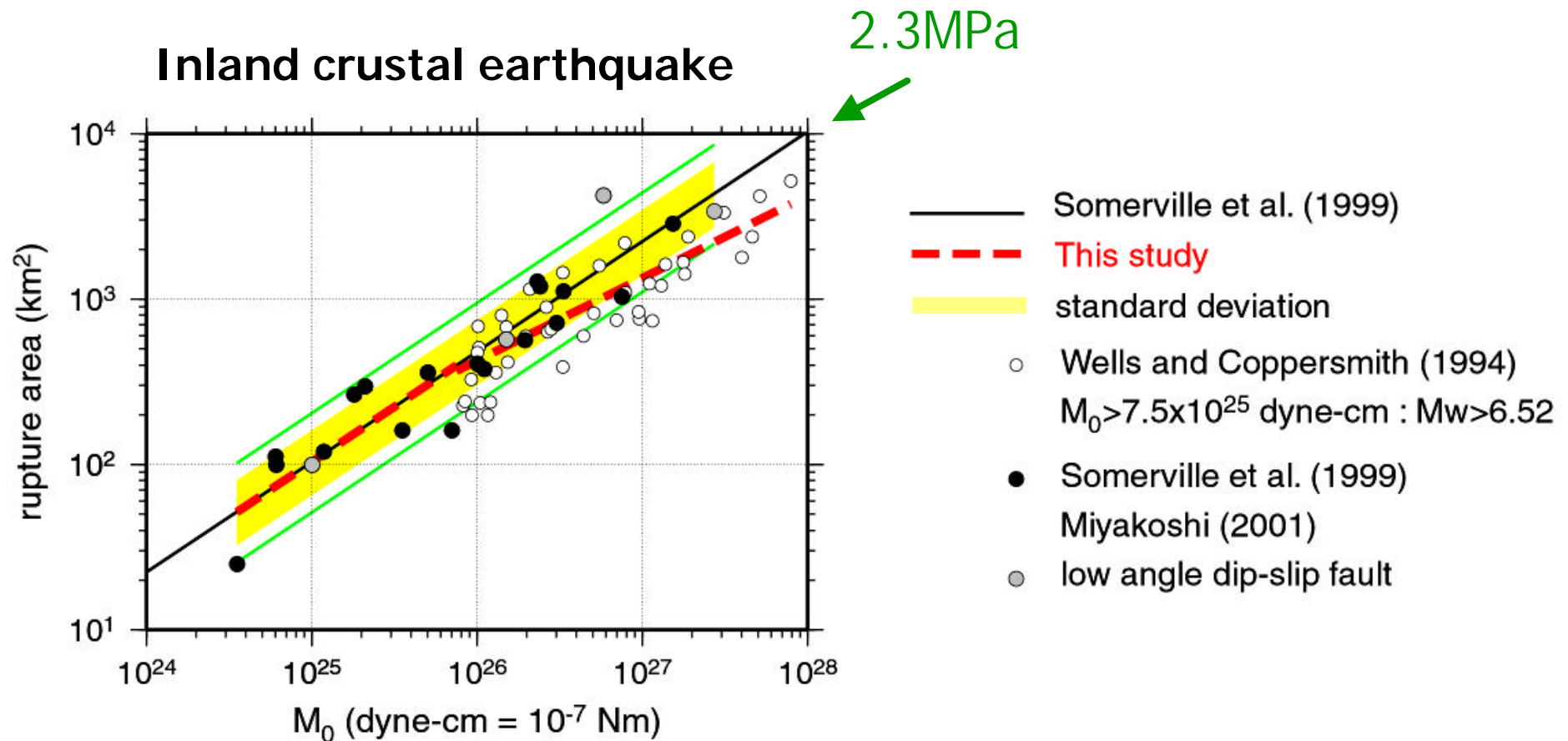
We propose deductive source model based on **multiple-asperity model**. (Previous recipe was based on **multiple-crack model**.)

Applicability of the recipe is examined for the 2000 Tottori earthquake using stochastic Green's function method (Kamae et al., 1991)



# Empirical Relationships for Outer Fault Parameters

## - Total Rupture Area (S) and Seismic Moment ( $M_0$ ) -



Irikura and Miyake (2001)



## Outer Fault Parameters

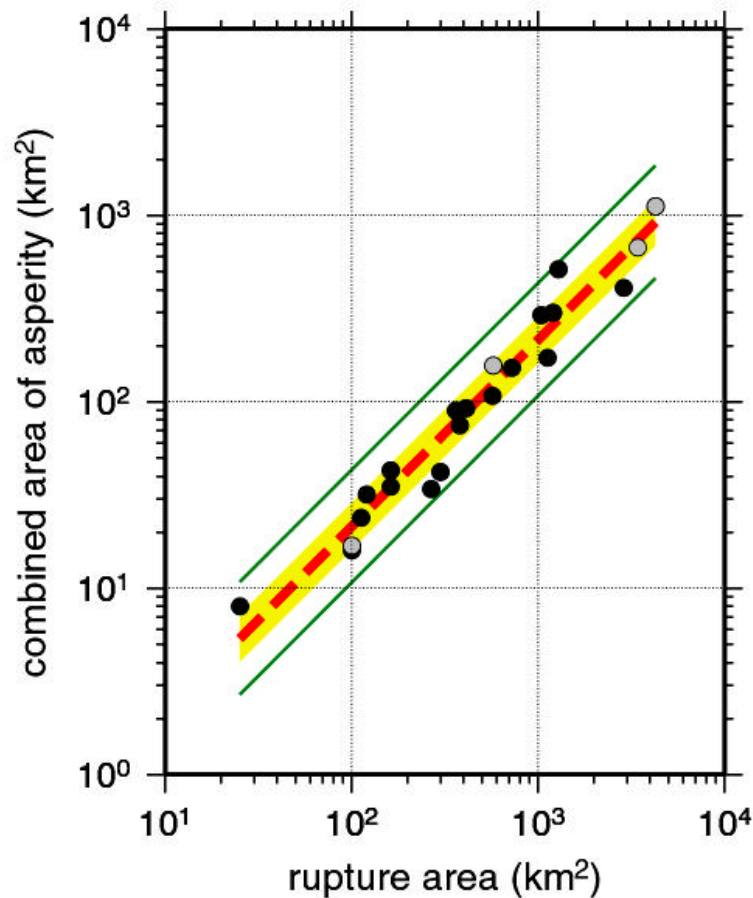
- Step 1: **Total rupture area** ( $S$ ) is given by products of total fault length ( $L$ ) and fault width ( $W$ ).
- Step 2: **Average static stress-drop** ( $\Delta\sigma_c$ ) on the fault is assumed. (inland crustal earthquake: about 2.3MPa)
- Step 3: **Total seismic moment** ( $M_0$ ) is estimated by  $S$  and  $\Delta\sigma_c$  assuming circular crack (Eshelby, 1957).

$$M_0 = \frac{16}{7\pi^{1.5}} \Delta\bar{\sigma}_c \cdot S^{1.5}$$

# Empirical Relationships for Inner Fault Parameters (1)

## - Combined Asperity Size ( $S_a$ ) and Total Rupture Area ( $S$ ) -

### Inland crustal earthquake



$$S_a = 0.29 S \quad (+ \text{ S.D.})$$

$$S_a = 0.215 S \quad (\text{average})$$

$$S_a = 0.16 S \quad (- \text{ S.D.})$$

--- This study

standard deviation

● Somerville et al. (1999)

● Miyakoshi (2001)

○ low angle dip-slip fault

Irikura and Miyake (2001)

## Inner Fault Parameters (1)

■ **Step 4:** Combined area of asperities ( $S_a$ ) is estimated by the empirical relationship between  $S_a$  and  $S$ .

■ **Step 5:** Stress stop on asperity is calculated by equations for **multiple-asperity model**.

(inland crustal earthquake: about 10.5MPa)

$$\Delta \mathbf{S}_a = \Delta \overline{\mathbf{S}}_c \cdot \frac{S}{S_a}$$

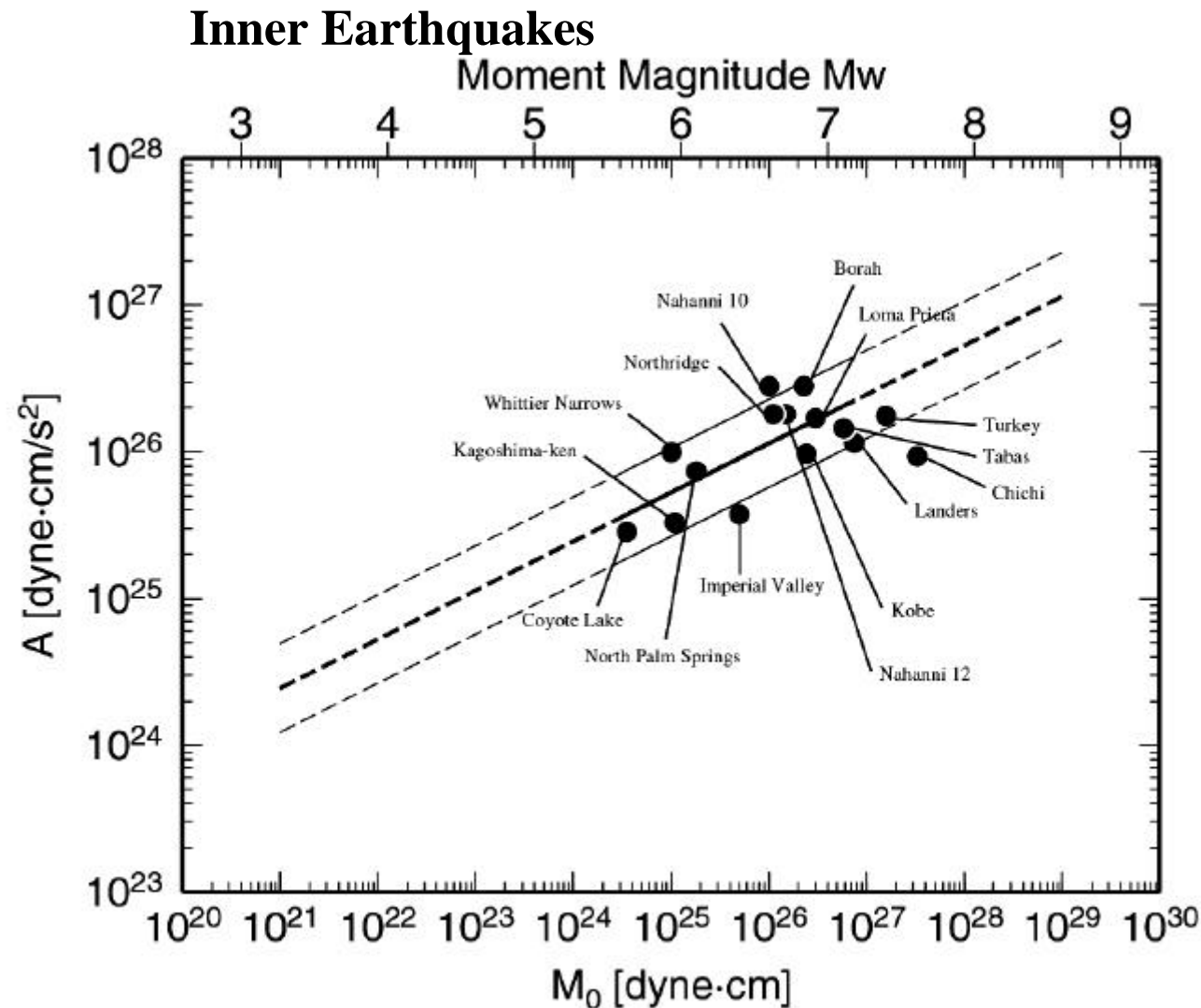
■ **Step 6:** Average slip for each asperity is estimated.

$$D_a^i = C \cdot \frac{\Delta \mathbf{S}_a}{m} \cdot r_i$$

■ **Step 7:** Number of asperities is defined by **Step 6**.

# Empirical Relationships for Inner Fault Parameters (2)

## - Short-period Source Spectra Level (A) and $M_0$ -



Dan et al. (2002)

## Inner Fault Parameters (2)

- Stress drop on asperity ( $\Delta\sigma_a$ ) is treated as effective stress ( $\sigma_a$ ) on asperity.
- **Step 8:** Summation of effective stress on asperities ( $\sigma_a$ ) and background slip area ( $\sigma_b$ ) is constrained by the empirical relationship between short-period spectral level and  $M_0$ .

$$A_0 = \sqrt{\sum_{i=1}^N \underbrace{(A_{0i}^a)^2}_{\text{asperities}} + \underbrace{(A_{0i}^b)^2}_{\text{background}}}$$

$$A_0^a = 4p b v_R \cdot S_a \cdot r$$

$$= 4\sqrt{p} b v_R \cdot S_a \cdot \sqrt{S_a}$$

Then  $A_0^a \propto M_0^{1/3}$

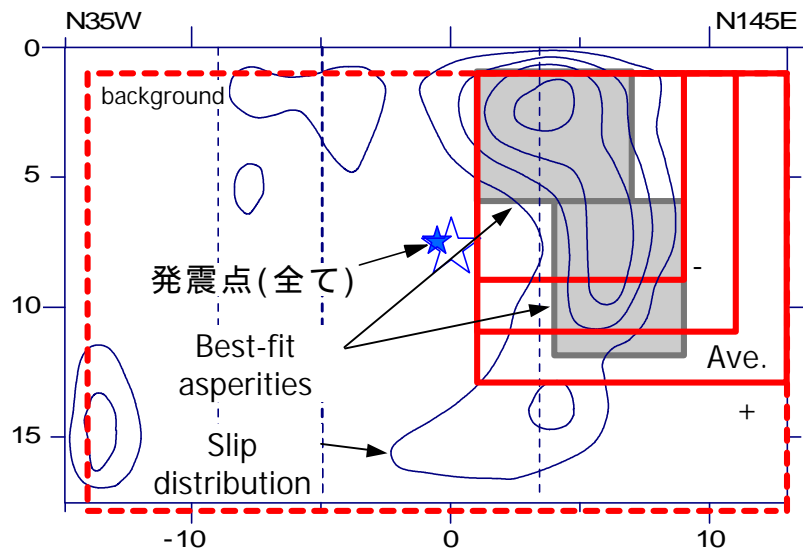
because  $(S_a/S)^{1/2} = \text{const}$  and  $S^{1/2} \propto M_0^{1/3}$

- **Step 9:** parameterization of slip velocity time functions

# Applicability of the Recipe

- 2000 Tottori-ken Seibu Earthquake: Mw6.6 -

## Deductive source model

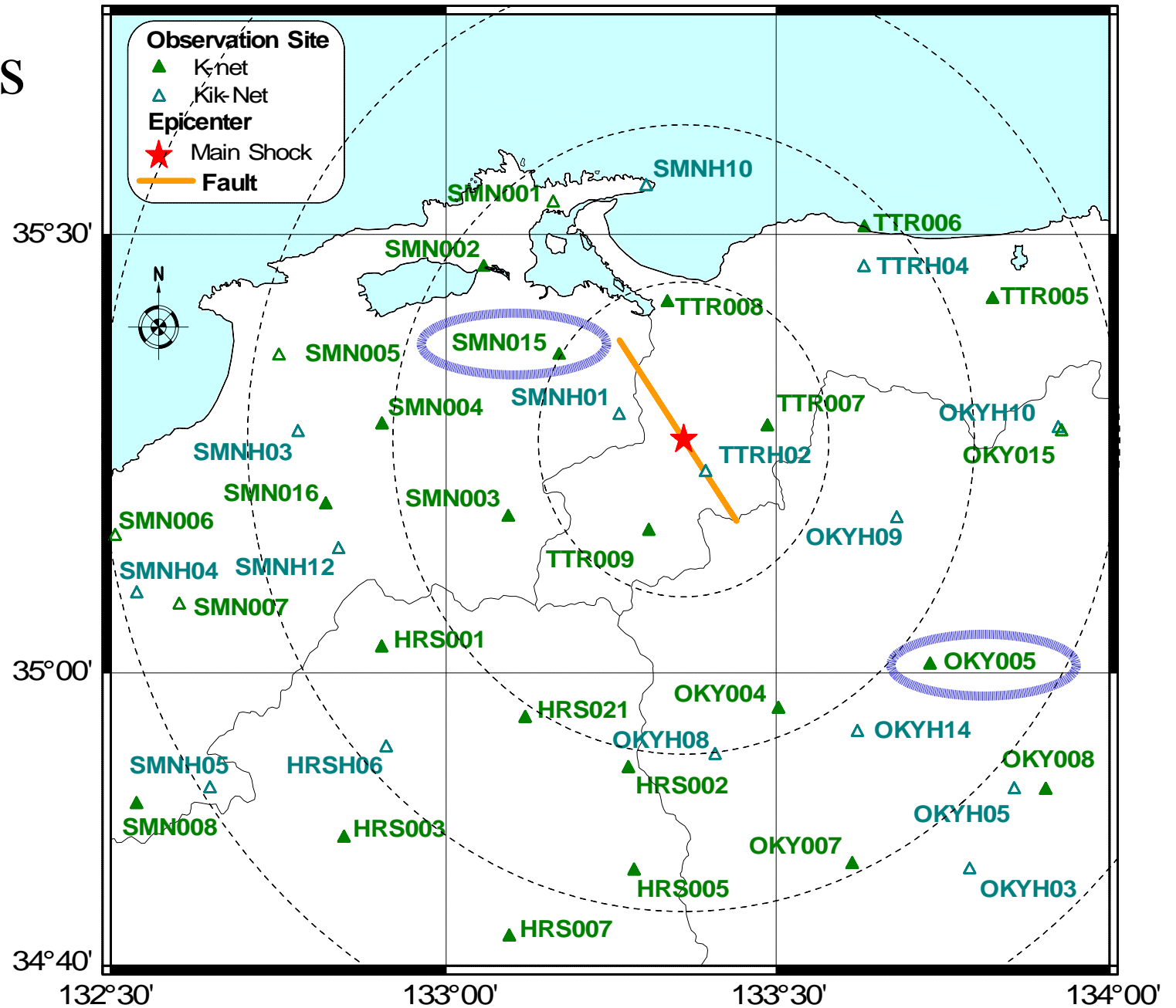


Effective stress on asperity and background is variable.

## Source parameters obtained by the recipe

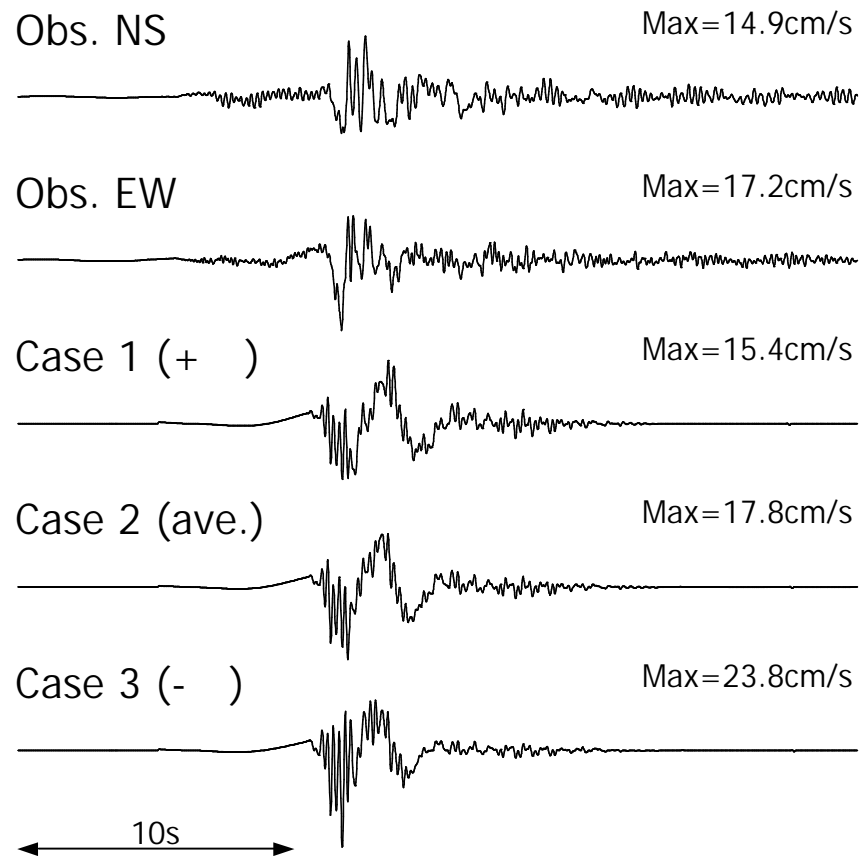
		Case 1 (+ )	Case 2 (ave.)	Case 3 (- )
total	Mo	9.6	9.6	9.6
	S	468	468	468
		2.3	2.3	2.3
asperity	Mo	5.8	4.3	3.2
	S <sub>a</sub>	141	105	78
	a	7.7	10.3	13.8
	a	1.32	1.13	0.98
Back ground	Mo	3.8	5.3	6.4
	S <sub>b</sub>	327	363	390
	b	5.1	4.0	2.2
	b	2.01	2.11	2.18
		Mo (10 <sup>25</sup> × dyne·cm), S (km <sup>2</sup> ), (MPa), (s)		

# Stations

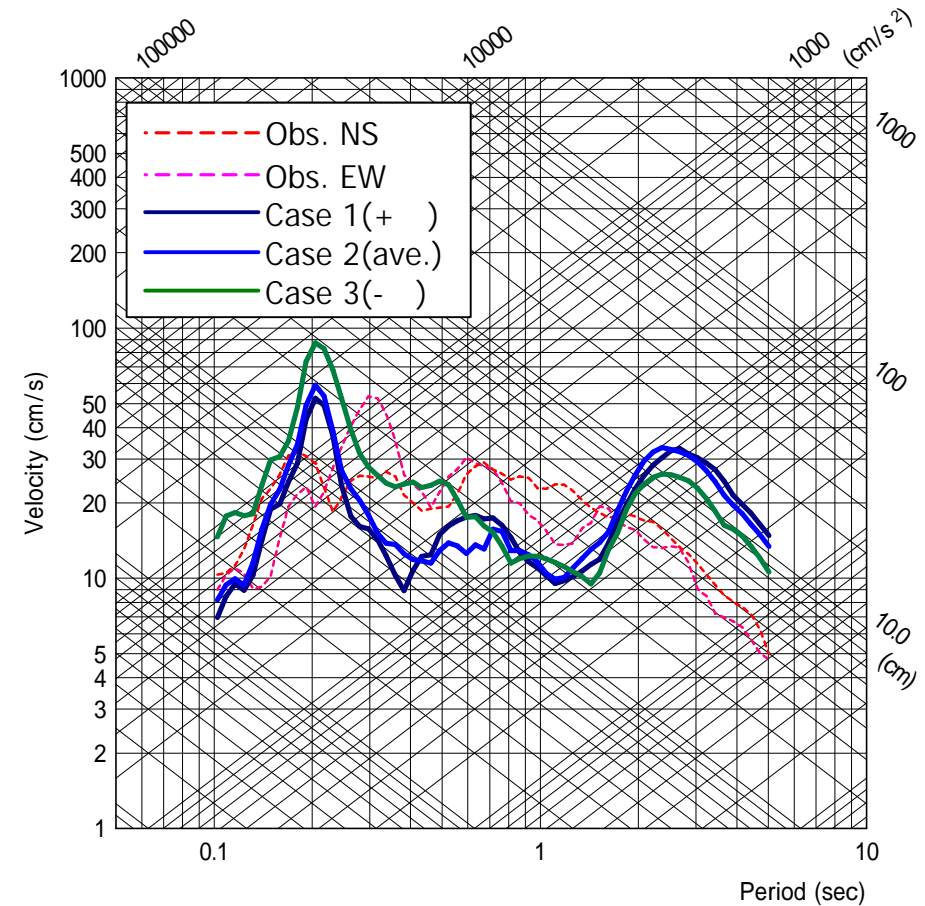




## Velocity at OKY005 (forward direction)

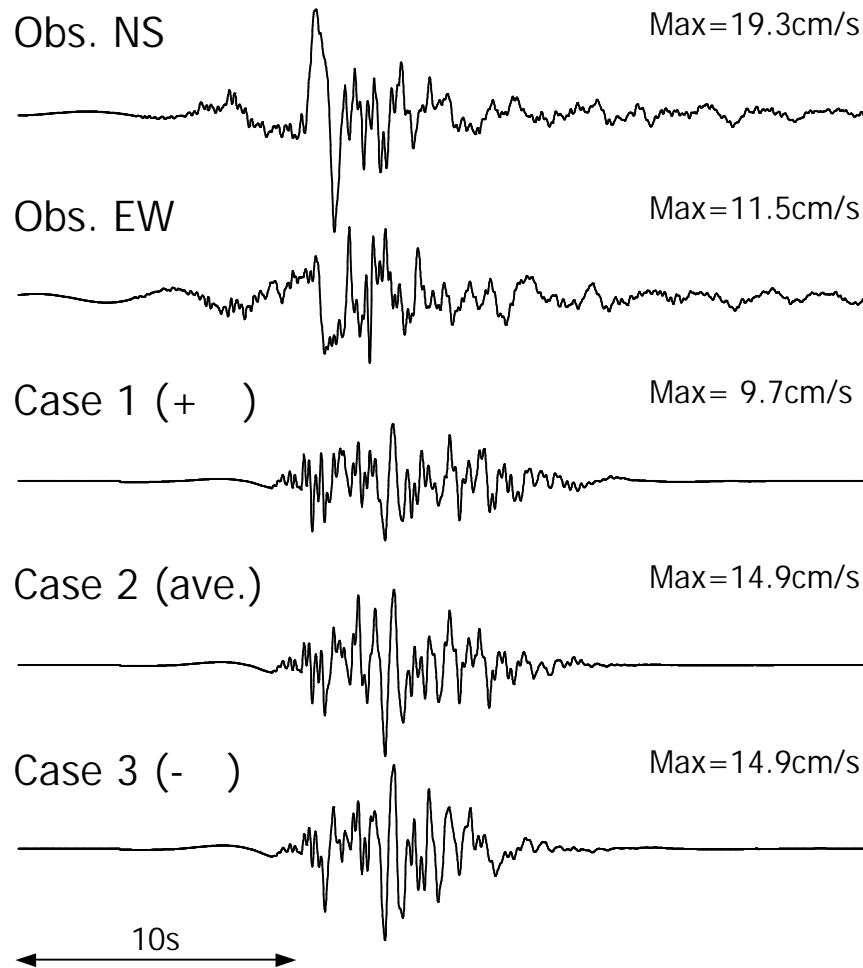


## Acceleration Response Spectra at OKY005 ( $h=0.05$ )

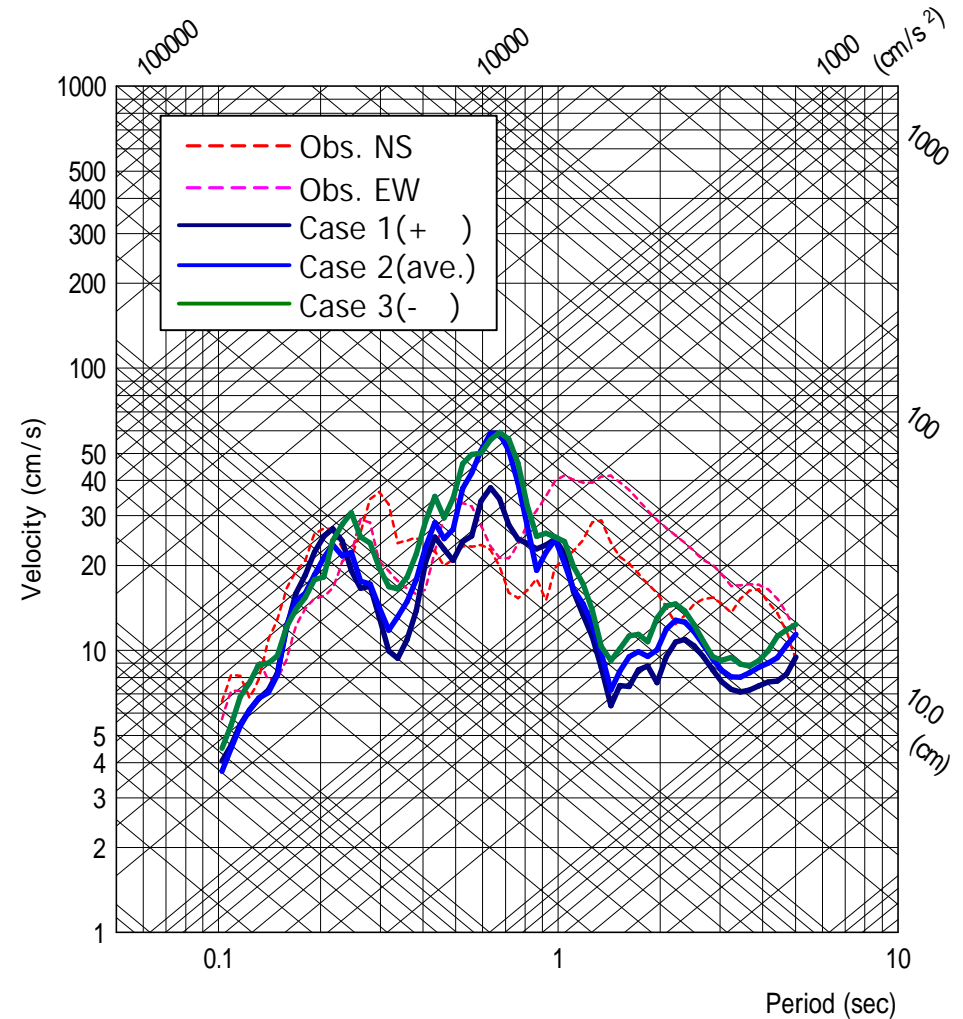


Ikeda et al. (2002)

## Velocity at SMN015 (backward direction)



## Acceleration Response Spectra at SMN015 ( $h=0.05$ )

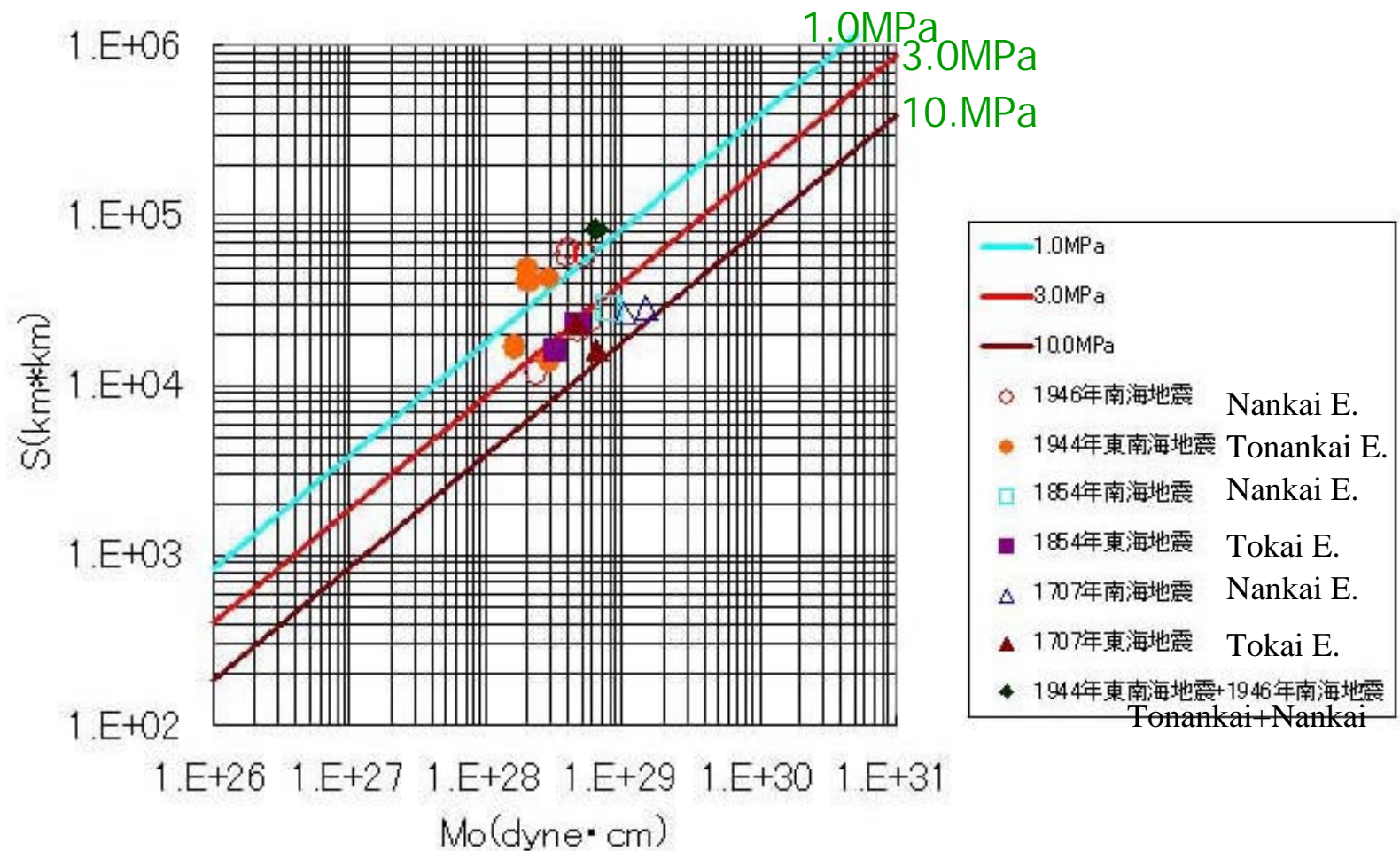


Ikeda et al. (2002)

# Empirical Relationship for Outer Fault Parameters

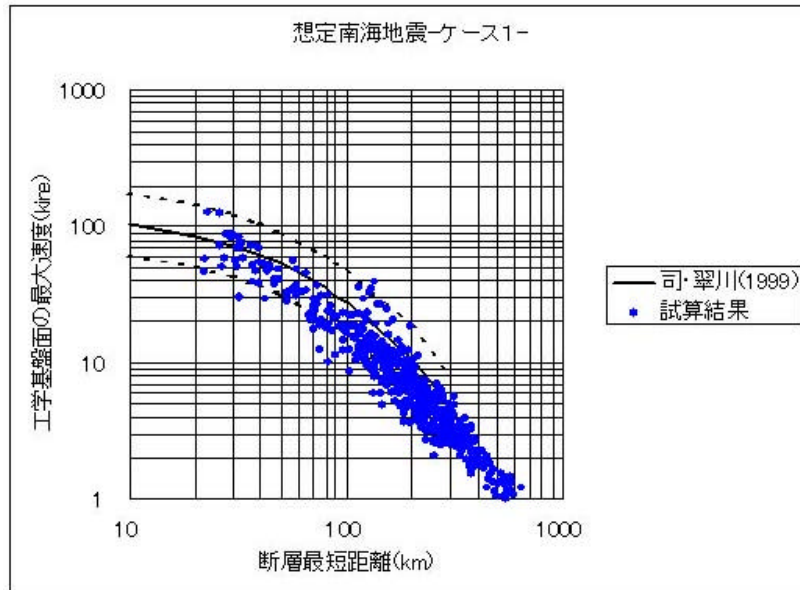
## - Total Rupture Area (S) and Seismic Moment (Mo) -

### - Subduction Earthquakes along Nankai Trough-



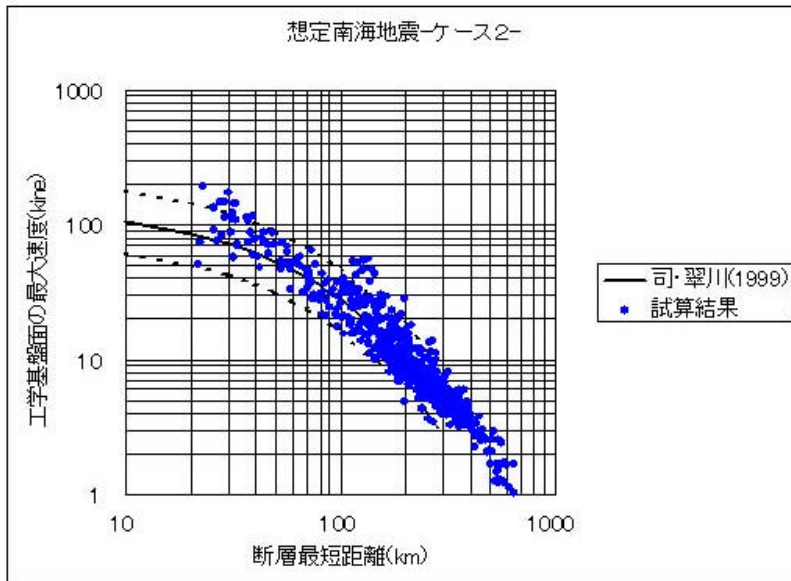
Earthquake Research Committee(2001)

# Attenuation Curve for PGV



Case 1

Effective stress on asperities = 10.1MPa



Case 2

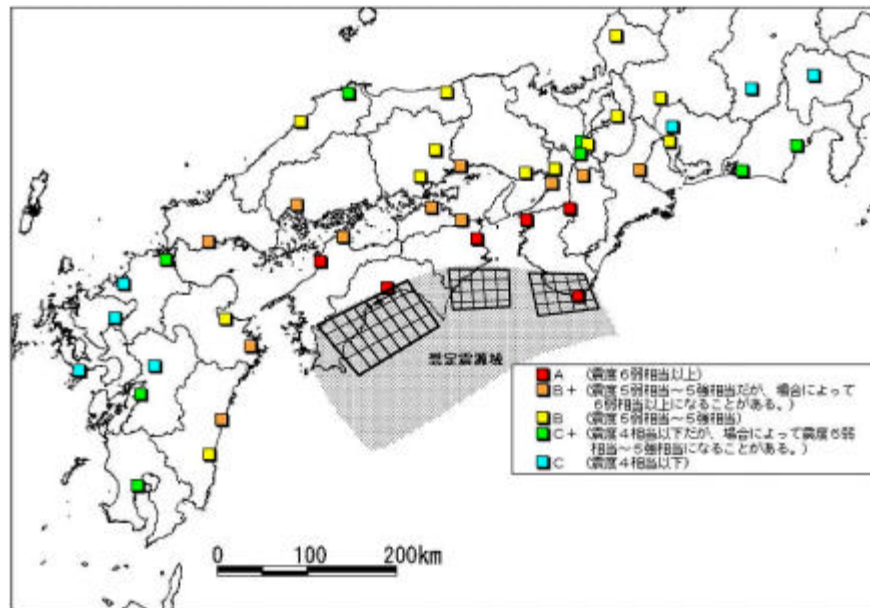
Effective stress on asperities = 20.1MPa

Earthquake Research Committee (2001)

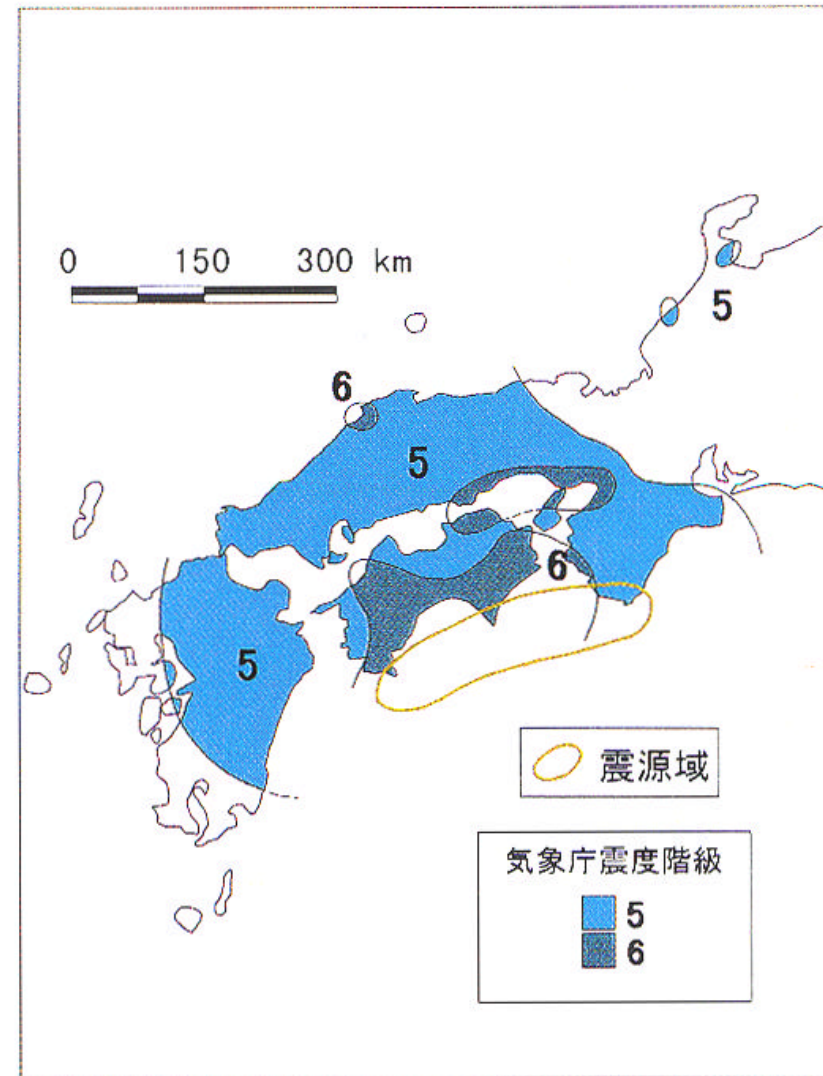


## Seismic Intensity for the 1854 Ansei Nankai Earthquake

## Seismic Intensity for Hypothetical Nankai Earthquake

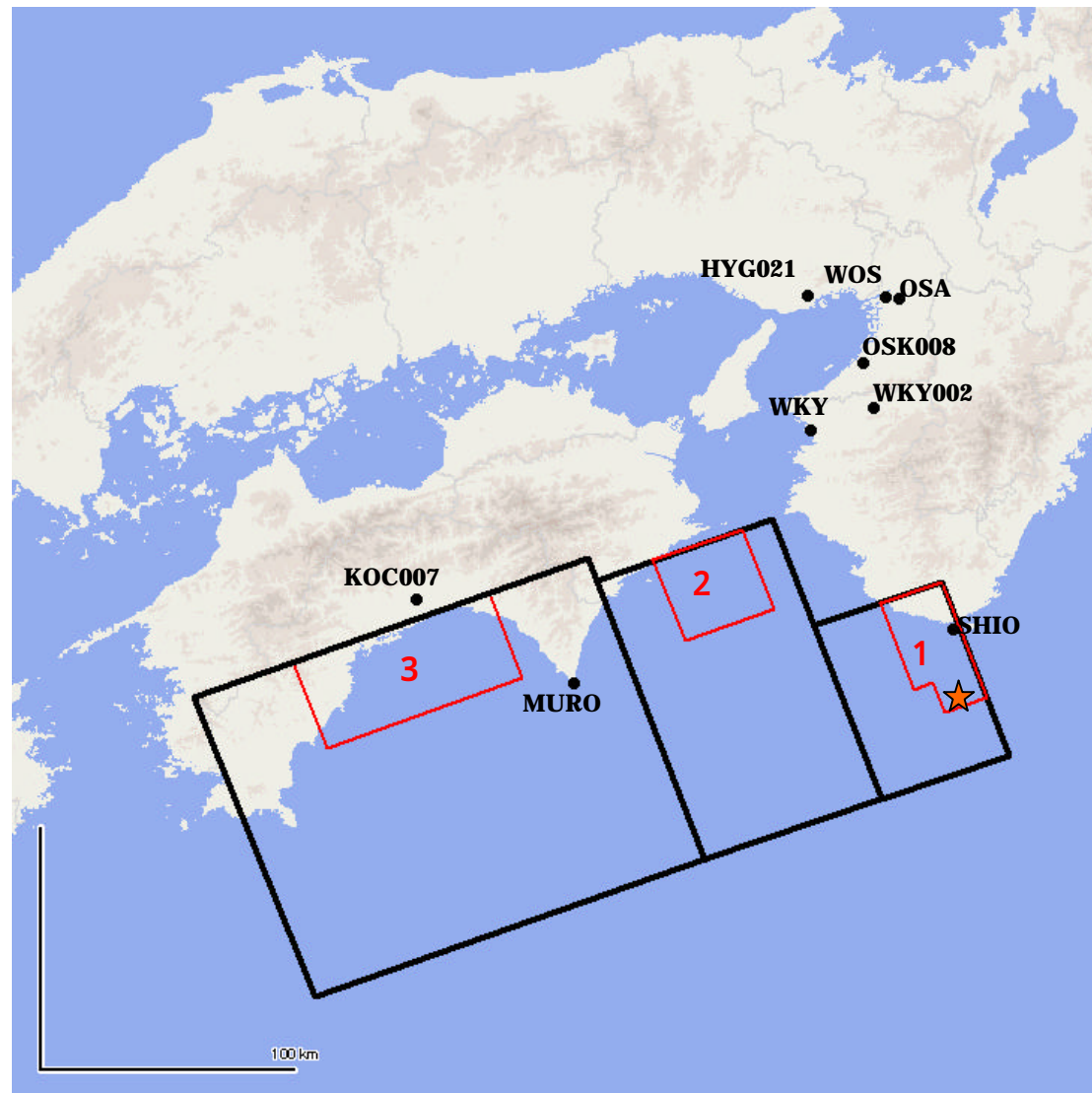


Earthquake Research Committee (2001)



Earthquake Research Committee (1999)

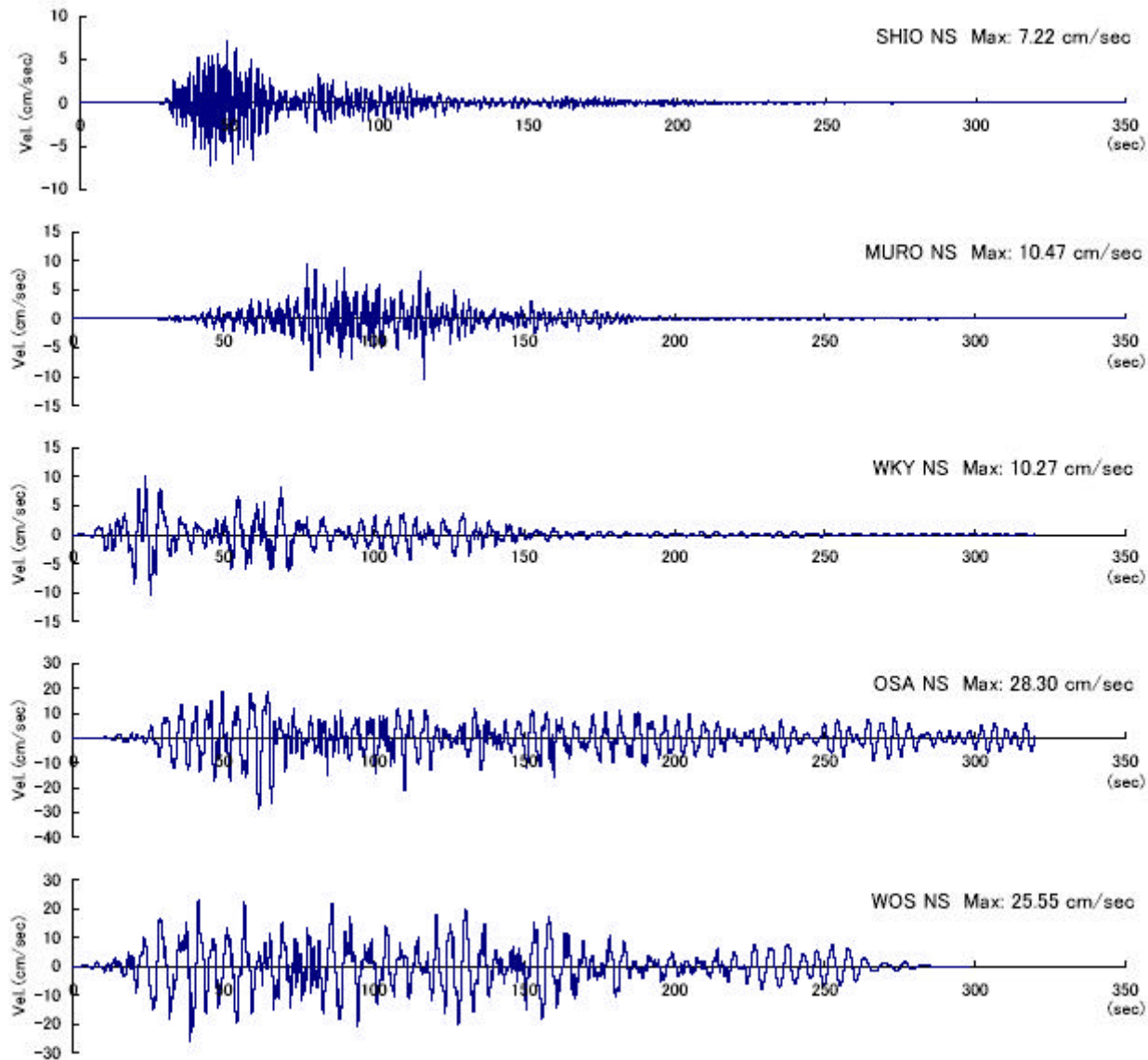
## *Source Model of Hypothetical Nankai Earthquake*



- ★ Rupture starting point
- Asperities

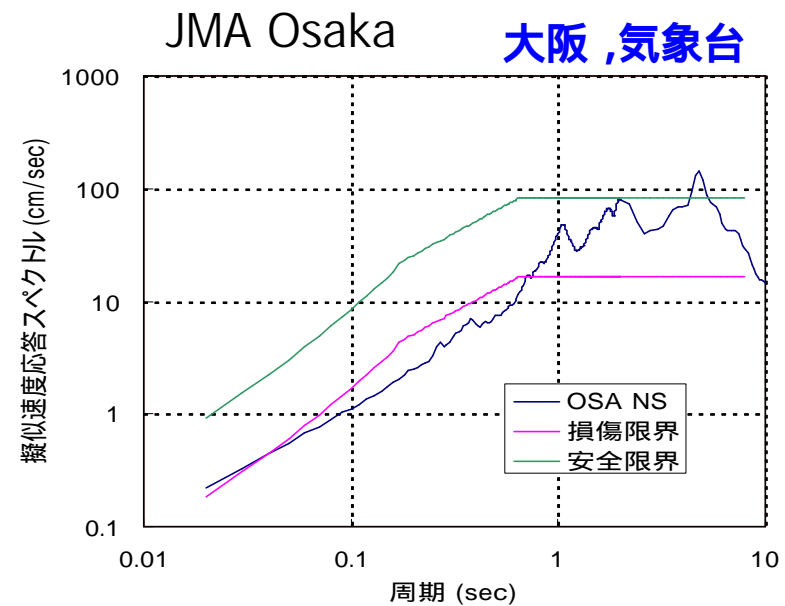
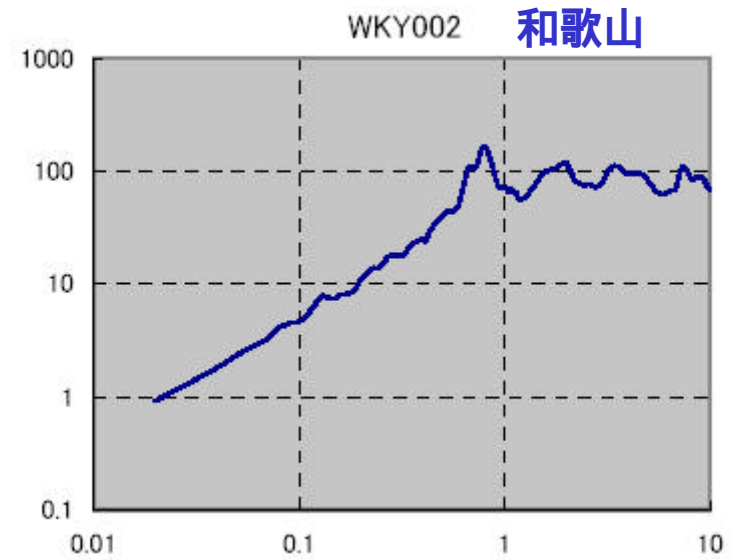
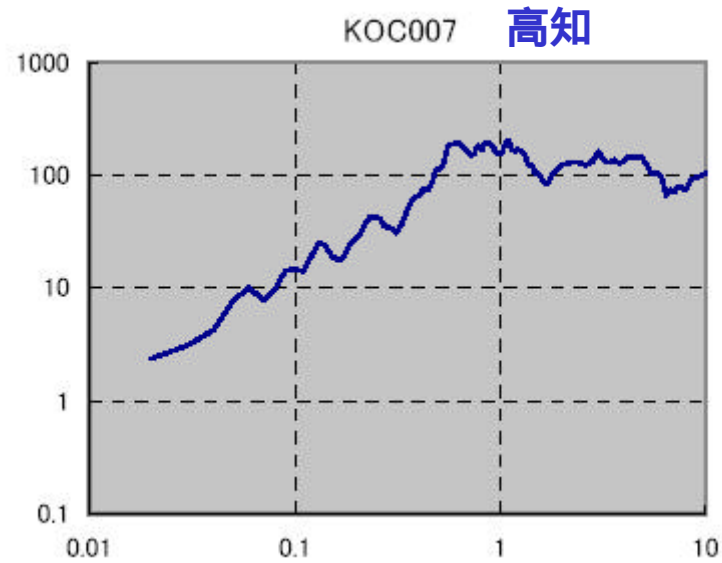
# *Synthetic Ground Motions from Hypothetical Nankai Earthquakes*

## *- Empirical Green's function Method -*





# *Pseudo-Velocity Response Spectra of Hypothetical Nankai Earthquake*



## Conclusions

- Our recipe for predicting strong ground motion only needs **total rupture area** ( $S$ ) and **average stress drop** ( $\Delta\sigma_c$ ) on the fault. Then, total seismic moment ( $M_0$ ), and the size and effective stress of asperities are given.
- Effective stress is differently estimated for **multiple-crack model** and **multiple-asperity model** in case of number of asperities increasing.
- The maximum amplitude of predicted motions are within a factor of 0.5 to 2.0 for  $1\sigma$  variance of the inner fault parameters.

# Asperity Model and Crack Model

## Case 1. single asperity

short period level

$$A_{0asperity}^1 = 4pbv_R \Delta s_a a$$

long period level

$$M_0^1 = \frac{16}{7} \Delta s_a a^2 R$$

stress drop

$$a = (7/16) M_0 / (Rr^2)$$

asperity

short period level

$$A_{0crack}^1 = 4pbv_R \Delta s_c a$$

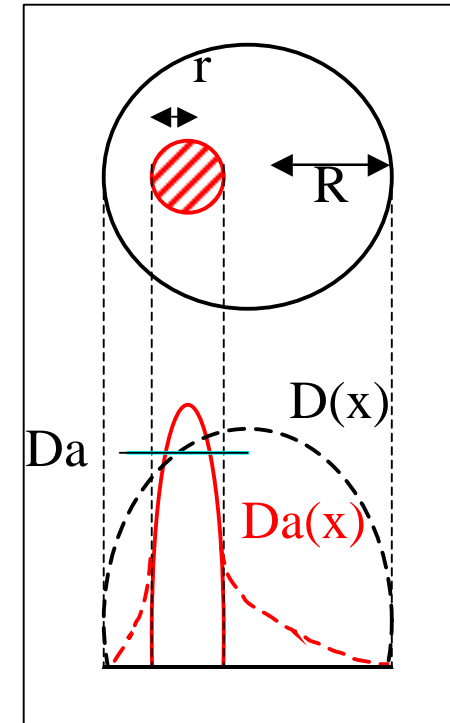
long period level

$$M_{0crack}^1 = \frac{16}{7} \Delta s_c a^3$$

stress drop

$$\Delta s_c = \frac{7p^{3/2}}{16} \frac{Mo_a}{S_a^{3/2}}$$

crack



$$r \ll R$$

$\Delta\sigma$  for single asperity (=9.5MPa) =  $\Delta\sigma$  for single crack (=9.6MPa)

# Asperity Model and Crack Model

## Case 2. multiple asperities

short period level

$$A_0^N{}_{\text{asperity}} = \left\{ \sum_{i=1}^N (4pbv_R \Delta \mathbf{s}_{ai} a_i)^2 \right\}^{\frac{1}{2}} = 4pbv_R \Delta \mathbf{s}_{ai} a$$

long period level

$$M_0^N = \sum_{i=1}^N \left( \frac{16}{7} \Delta \mathbf{s}_{ai} a_i^2 R_i \right) = \frac{16}{7} \Delta \mathbf{s}_{ai} a^2 R$$

stress drop

$$\Delta \mathbf{s}_a = \Delta \mathbf{s}_{ai} = \frac{7}{16} \frac{M_0^1}{a^2 R}$$

multiple  
asperity model

short period level

$$A_0^N{}_{\text{crack}} = \left\{ \sum_{i=1}^N (4pbv_R \Delta \mathbf{s}_{ci} a_i)^2 \right\}^{\frac{1}{2}} = 4pbv_R \Delta \mathbf{s}_{ci} a$$

long period level

$$M_0^N{}_{\text{crack}} = \sum_{i=1}^N \left( \frac{16}{7} \Delta \mathbf{s}_{ci} a_i^3 \right) = \frac{1}{a} \frac{16}{7} \Delta \mathbf{s}_{ci} a^3 \quad (1 < a < \sqrt{N})$$

stress drop

$$\frac{\Delta \mathbf{s}_{ci}}{\Delta \mathbf{s}_c} = \frac{A_0^N{}_{\text{crack}}}{A_0^1{}_{\text{crack}}} = a \frac{M_0^N{}_{\text{crack}}}{M_0^1{}_{\text{crack}}}$$

multiple crack  
model

# What's New ? -Stress drop on asperity-

multiple-crack model      multiple-asperity model

$$\Delta \mathbf{s}_c = \frac{7}{16} \frac{M_{0asp}}{r^3}$$

$$\Delta \mathbf{s}_a = \frac{7}{16} \frac{M_0}{Rr^2}$$

n=1:                      9.6MPa

10.5MPa

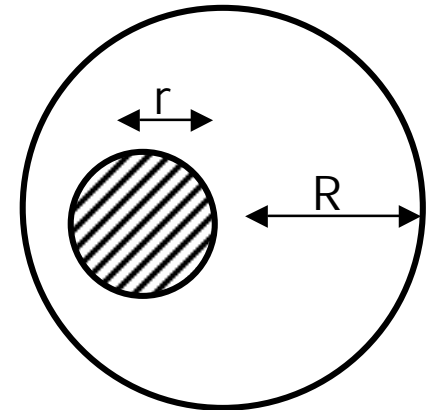
n=2:      9.6 - 13.6MPa

10.5MPa

n=N:      9.6 -  $9.6 \sqrt{N}$  MPa

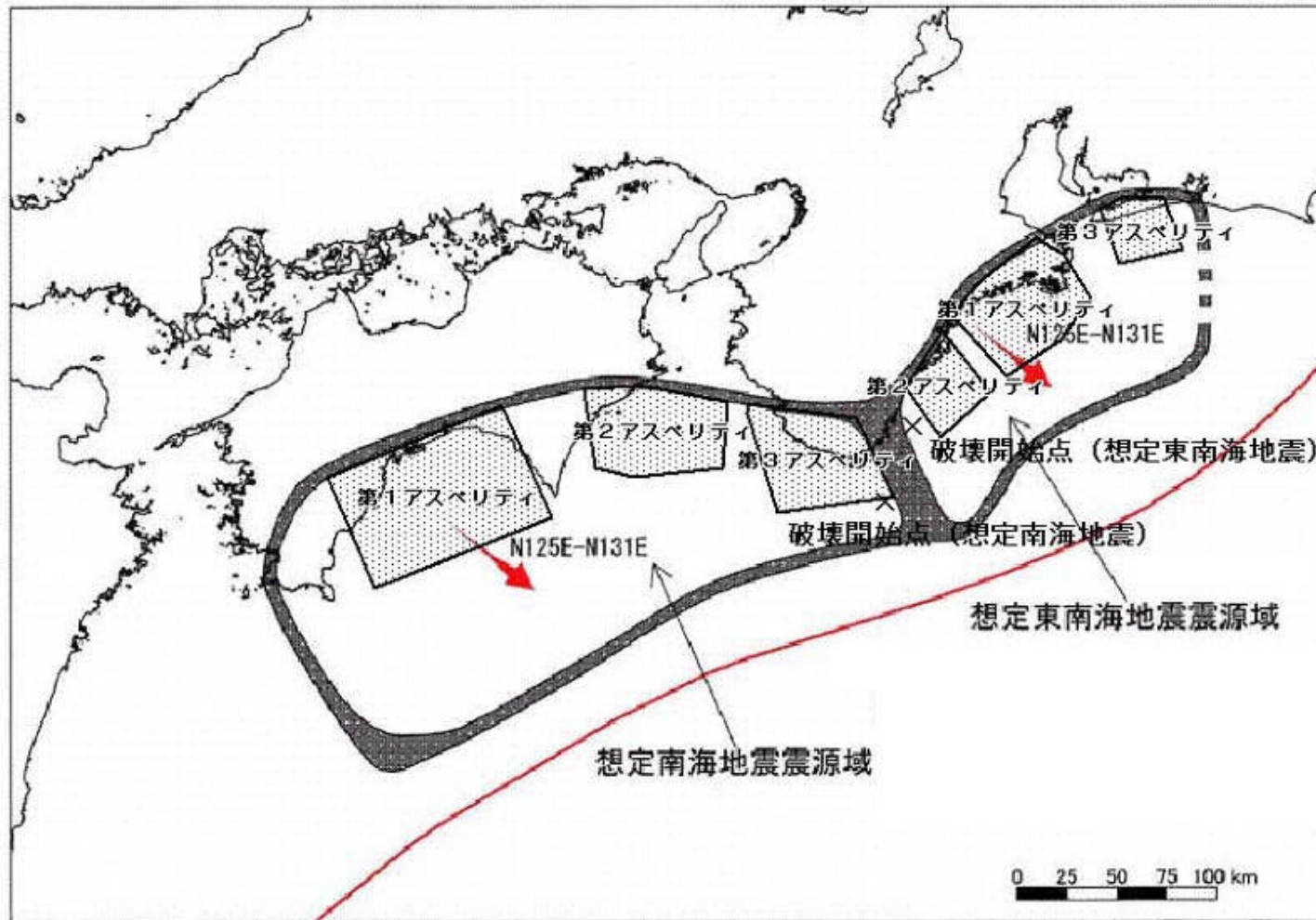
10.5MPa

For  $\pi r^2 / \pi R^2 = 0.22$



# Applicability of the Recipe

-Hypothetical Tonankai and Nankai earthquakes-



Earthquake Research Committee (2001)